

*Isotropic Turbulence*

*Visualization by NCSA's  
advanced applications  
support group*

*Atms 502, CSE 566*

# *Numerical Fluid Dynamics*

*MAR. 12, 2019*

**ATMS 502**  
**CSE 566**

Tuesday,  
12 March 2019

Class #17

## Plan for Today

- 1) Program 4, continued
  - Sequence & testing
- 2) Skamarock & Klemp
  - Introductory material missing last time
- 3) Parallel performance
  - Fundamentals - introduction

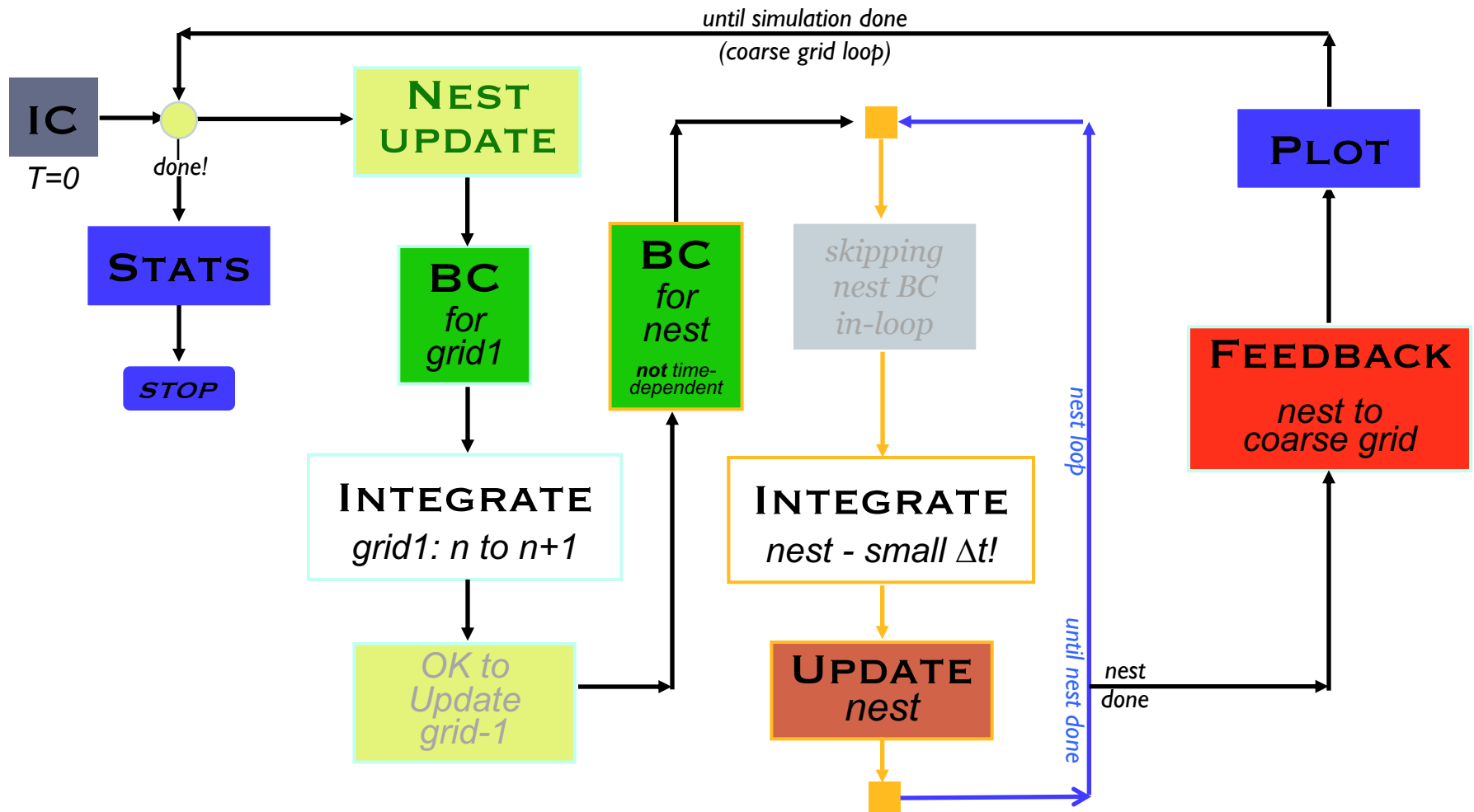
# Program 4: suggested development

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- Restore the rotating flow initial conditions (pgm2)
- Add nested-grid  $s1$ ,  $s2$ ,  $u$ ,  $v$  arrays
- Nest-testing:
  - call your “truncation-error & nest-locating” routine after  $IC$
  - call `dointerp()` to initialize the nest (fill nested  $s1$  array)
  - call `nestwind()` to fill the nested  $u/v$  arrays
  - plot: coarse & nested grid arrays! Does they make sense?
    - ✦ Plot nest position on coarse grid plots. Plot all fields – all OK?
- Fake-nest
  - Main time step loop: every 5 steps, call the above routines to “re-initialize” the nest; show nest box on coarse grid plots.

# Program #4: main routine

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# Skamarock & Klemp

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THE MISSING INTRODUCTION  
FROM LAST TIME.

# Local vs. Global refinement

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- Global: *move points*
  - Advantages:
    - ✦ Key: smoother transition between high, low resolution (less wave-reflection)
  - Disadvantages:
    - ✦ complex solver due to irregularity of grid
    - ✦ grid regenerated every time step
    - ✦ increased resolution in one area reduces it elsewhere.
    - ✦ time step set by that in highest resolution region
- Local: *add points*
  - Advantages:
    - ✦ Simple(r) solver
    - ✦ less development time
    - ✦ easier parallelization
    - ✦ Different time steps for different grid resolutions - more efficient.
  - Disadvantages:
    - ✦ Abrupt resolution changes cause noise e.g. wave reflection

# Nesting strategy

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- Identification & clustering

## Richardson Extrapolation

$$\tau \approx \frac{Q_h^2(u(x,t)) - Q_{2h}(u(x,t))}{2^{q+1} - 2}$$

- In English! The procedure is:
  - Take **two** time steps as usual
  - Take one **giant** step with  $2\Delta x, 2\Delta t$
  - Difference approximates the **truncation error**
  - “... if the solution is smooth”

“Adaptive Grid Refinement for Numerical Weather Prediction” - *William Skamarock, Stanford, 1987*

# Richardson extrapolation (more)

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- Richardson extrapolation – notes
  - From Skamarock – Stanford Dissertation, pp. 11-12 ([link](#))
  - In Richardson extrapolation method,  $Q_h$  “is an operator representing the finite difference scheme
  - “ $Q_h^2$  is the operator  $Q_h$  twice applied to  $u(x,t)$
  - Advantages of this method to estimate truncation error:
    - ✦ Exact form of truncation error need not be known
    - ✦ For systems of equations with several variables, calculating truncation error accurately “can be very difficult”
    - ✦ The same solver is used to integrate equations & estimate error
    - ✦ Estimator is independent of finite difference method and PDE



# Nesting strategy

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- Identification
    - grid points exceeding some threshold, e.g. truncation error
  - Clustering
    - fit to enclose points
    - general AMR allows overlapping grids, arbitrary orientation
  - Nest: Initial conditions
    - Interpolated from coarse grid, or existing nests
  - Nest: Bound. conditions
    - Time dependent
      - ✦ from coarse grid, using current and 'next' step.
    - Spatial dependence
      - ✦ interpolated from coarse grid. in our case, nest BC overlap with coarse points
- 
- Feedback: nest to coarse grid
    - Average nest interior to coarse points

# Finite volume method; van Leer

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## Overview:

- van Leer published five papers between 1973-79
- J. Comp. Phys., vol. 23, 276-299 (1977):

“Towards the ultimate conservative difference scheme: IV. A new approach to numerical convection”

## Handout:

- Hourdin and Armengaud, 1999: Use of finite volume methods for atmospheric advection of trace species
  - flux forms
  - monotonicity
  - "approximating the sub-grid-scale distribution by a polynomial" (HA99 p. 823)

# Introduction: Parallel performance

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Some figures from  
High Performance Computing  
by David Kuck (Oxford Press, NY)

Others: LLNL pages on parallel computing:  
[https://computing.llnl.gov/tutorials/parallel\\_comp/](https://computing.llnl.gov/tutorials/parallel_comp/)

# Really?

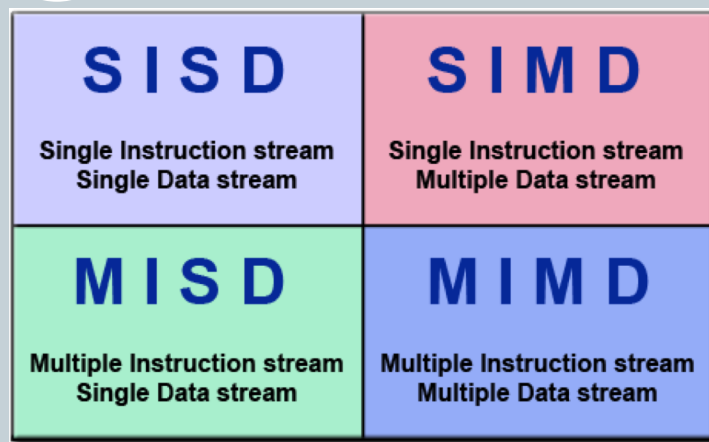
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- Yes.
  - As computational scientists, some knowledge of how computers *work* gives you advantages over those who don't
  - We'll discuss *only* the basics. More information..
    - ✦ *U.I. Computer Science*, [cs.illinois.edu](http://cs.illinois.edu)
    - ✦ *Computational Science & Engineering*, [www.cse.illinois.edu](http://www.cse.illinois.edu)
      - UI Ph.D computer science ranked 5<sup>th</sup> in U.S.; Engineering, 4<sup>th</sup> (world)
- This information may help you answer questions like:
  - Why did my code not run (*even*) faster with more processors?
  - Why did the size of my grid make such a difference?
  - What delays / difficulties am I likely to encounter?
  - How do I make best use of a computer cluster to do my work?

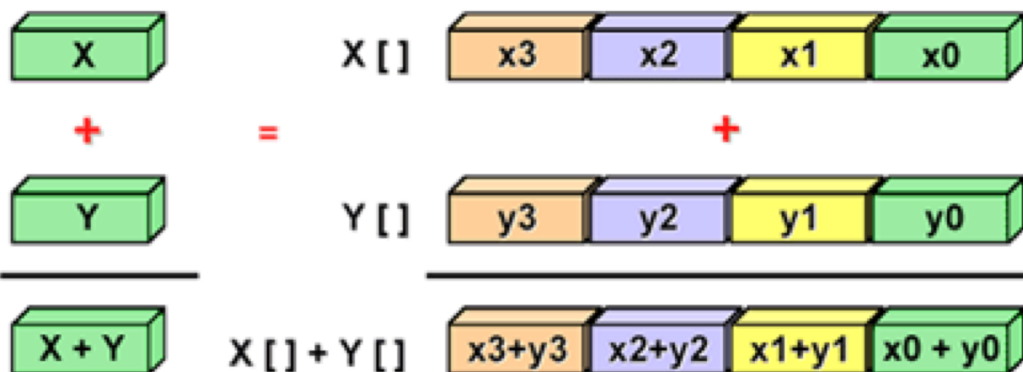
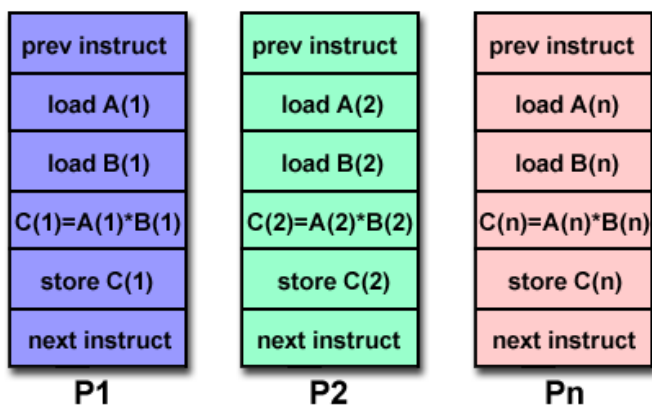
# Introductory concepts

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- Types of computing: Flynn's taxonomy
- Doing the same task on all cores is *SIMD*



## *SIMD* computing

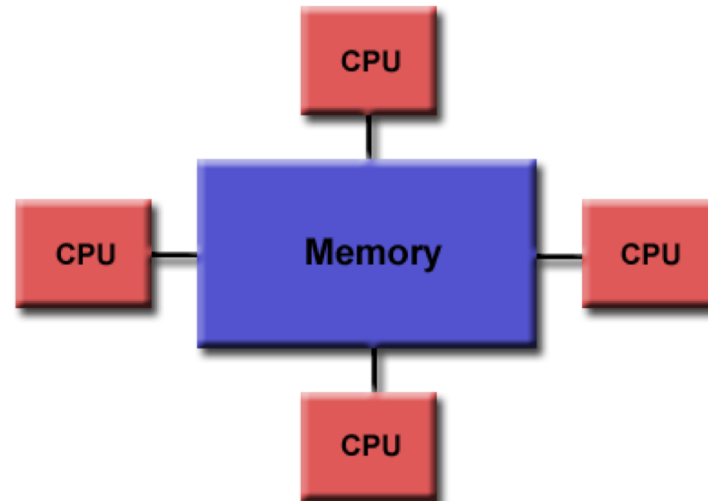


# Shared vs. Distributed Memory Architecture

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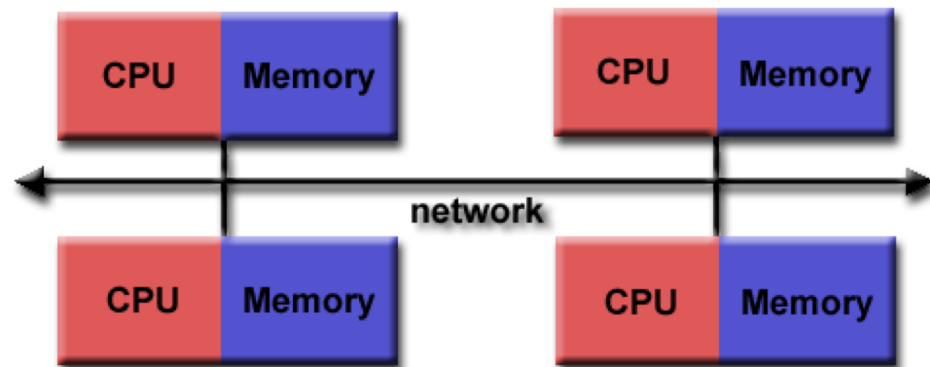
- **Shared memory**

- multiple processors access all memory as *global address space*.



- **Distributed memory**

- processors have local memory
- programmer handles data movement explicitly.



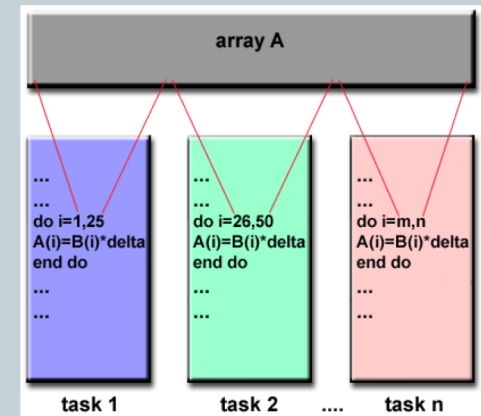
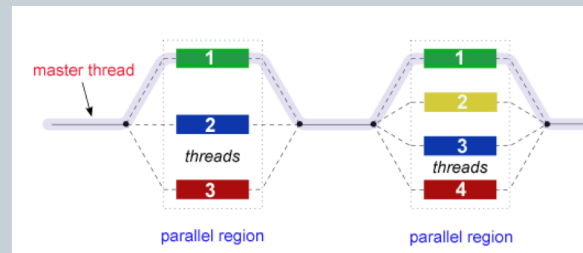
# Shared vs. Distributed Memory Parallelism

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- **Shared** memory parallelism: *OpenMP*

- main program creates tasks (*threads*) that can be run concurrently (simultaneously).

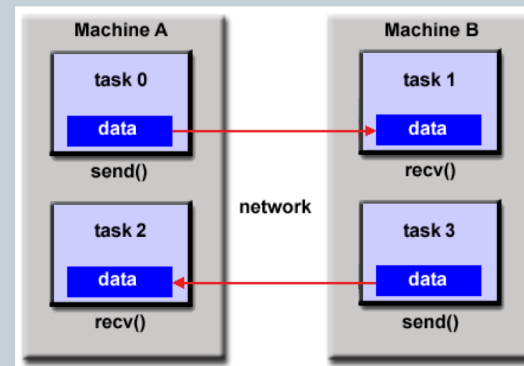
- ✦ in *loop-level* parallelism, threads handle loop tasks.



- **Distributed** memory / Message passing interface: *MPI*

- Each task uses local memory

- ✦ Data exchanged by sending and receiving messages
- ✦ Latest version is MPI 3.1



# Hybrid architectures & parallelism

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- **Hybrid parallelism** combines OpenMP threads model with the message passing (MPI) model
  - threads handle local (on-node) data
  - communication between nodes is done via MPI

