

Isotropic Turbulence
Visualization by NCSA's advanced applications support group

Atms 502, CSE 566

Numerical Fluid Dynamics

MAR. 12, 2019

vis.ncsa.illinois.edu/gallery.html

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Plan for Today

- 1) Program 4, continued
 - Sequence & testing
- 2) Skamarock & Klemp
 - Introductory material missing last time
- 3) Parallel performance
 - Fundamentals - introduction

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Program 4: suggested development

- Restore the rotating flow initial conditions (pgm2)
- Add nested-grid s1, s2, u, v arrays
- Nest-testing:
 - call your "truncation-error & nest-locating" routine after IC
 - call dinterp0 to initialize the nest (fill nested s1 array)
 - call nestwind0 to fill the nested u/v arrays
 - plot: coarse & nested grid arrays! Does they make sense?
 - ✦ Plot nest position on coarse grid plots. Plot all fields -- all OK?
- Fake-nest
 - Main time step loop: every 5 steps, call the above routines to "re-initialize" the nest; show nest box on coarse grid plots.

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Program #4: main routine

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Skamarock & Klemp

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THE MISSING INTRODUCTION
FROM LAST TIME.

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Local vs. Global refinement

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C010: Adaptive mesh refinement • C047: Global refinement

- **Global: move points**
 - **Advantages:**
 - ✦ Key: smoother transition between high, low resolution (less wave-reflection)
 - **Disadvantages:**
 - ✦ complex solver due to irregularity of grid
 - ✦ grid regenerated every time step
 - ✦ increased resolution in one area reduces it elsewhere.
 - ✦ time step set by that in highest resolution region
- **Local: add points**
 - **Advantages:**
 - ✦ Simple(r) solver
 - ✦ less development time
 - ✦ easier parallelization
 - ✦ Different time steps for different grid resolutions - more efficient.
 - **Disadvantages:**
 - ✦ Abrupt resolution changes cause noise e.g. wave reflection

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Nesting strategy

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SKAMAROCK AND KLEMP

- Identification & clustering

Richardson Extrapolation

$$\tau \approx \frac{Q_h^2(u(x,t)) - Q_{2h}(u(x,t))}{2^{q+1} - 2}$$

- In English! The procedure is:
 - Take **two** time steps as usual
 - Take **one giant step** with $2\Delta x, 2\Delta t$
 - Difference approximates the **truncation error**
 - “... if the solution is smooth”

Adaptive Grid Refinement for Numerical Weather Prediction - William Skamarock, Stanford, 1987

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C008: Truncation error • C010: Adaptive mesh refinement • C021: Grid refinement strategy

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Richardson extrapolation (more)

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- **Richardson extrapolation – notes**
 - From Skamarock – Stanford Dissertation, pp. 11-12 ([link](#))
 - In Richardson extrapolation method, Q_h “is an operator representing the finite difference scheme
 - “ Q_h ” is the operator Q_h twice applied to $u(x,t)$
 - Advantages of this method to estimate truncation error:
 - ✦ Exact form of truncation error need not be known
 - ✦ For systems of equations with several variables, calculating truncation error accurately “can be very difficult”
 - ✦ The same solver is used to integrate equations & estimate error
 - ✦ Estimator is independent of finite difference method and PDE

SKAMAROCK AND KLEMP

Nesting strategy

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- **Identification**
 - grid points exceeding some threshold, e.g. truncation error
- **Clustering**
 - fit to enclose points
 - general AMR allows overlapping grids, arbitrary orientation

- **Feedback: nest to coarse grid**
 - Average nest interior to coarse points

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Finite volume method; van Leer

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NOTES – IN HANDOUTS LAST CLASS

Overview:

- van Leer published five papers between 1973-79
- J. Comp. Phys., vol. 23, 276-299 (1977):
 “Towards the ultimate conservative difference scheme: IV. A new approach to numerical convection”

Handout:

- Hourdin and Armengaud, 1999: Use of finite volume methods for atmospheric advection of trace species
 - flux forms
 - monotonicity
 - "approximating the sub-grid-scale distribution by a polynomial" (HA99 p. 823)

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Introduction: Parallel performance

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Some figures from High Performance Computing by David Kuck (Oxford Press, NY)

Others: LLNL pages on parallel computing:
https://computing.llnl.gov/tutorials/parallel_comp/

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Really?

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- **Yes.**
 - As computational scientists, some knowledge of how computers work gives you advantages over those who don't
 - We'll discuss *only* the basics. More information..
 - U.I. Computer Science, cs.illinois.edu
 - Computational Science & Engineering, www.cse.illinois.edu
 - UI Ph.D computer science ranked 5th in U.S.; Engineering, 4th (world)
- **This information may help you answer questions like:**
 - Why did my code not run (even) faster with more processors?
 - Why did the size of my grid make such a difference?
 - What delays / difficulties am I likely to encounter?
 - How do I make best use of a computer cluster to do my work?

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Introductory concepts

SISD
Single Instruction stream
Single Data stream

SIMD
Single Instruction stream
Multiple Data stream

MISD
Multiple Instruction stream
Single Data stream

MIMD
Multiple Instruction stream
Multiple Data stream

Types of computing: Flynn's taxonomy

- Doing the same task on all cores is **SIMD**

SIMD computing

prev instruction load A(1) load B(1) C(1)=A(1)*B(1) store C(1) next instruction P1	prev instruction load A(2) load B(2) C(2)=A(2)*B(2) store C(2) next instruction P2	prev instruction load A(n) load B(n) C(n)=A(n)*B(n) store C(n) next instruction Pn
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X

x0 x1 x2 x3

X []

+

Y

y0 y1 y2 y3

Y []

=

X + Y

x0+y0 x1+y1 x2+y2 x3+y3

X [] + Y []

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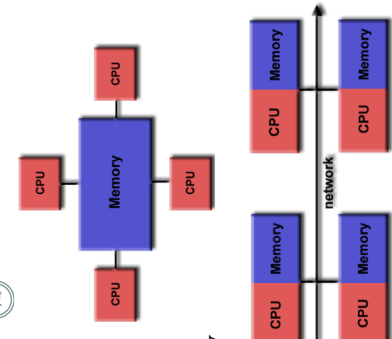
Shared vs. Distributed Memory Architecture

Shared memory

- multiple processors access all memory as *global address space*.

Distributed memory

- processors have local memory
- programmer handles data movement explicitly.



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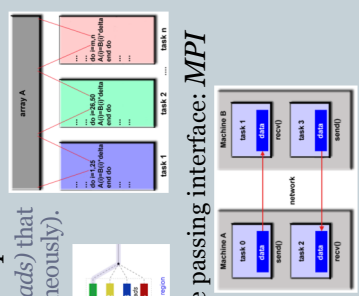
Shared vs. Distributed Memory Parallelism

Shared memory parallelism: OpenMP

- main program creates tasks (*threads*) that can be run concurrently (simultaneously).
 - in *loop-level* parallelism, threads handle loop tasks.

Distributed memory / Message passing interface: MPI

- Each task uses local memory
 - Data exchanged by sending and receiving messages
 - Latest version is MPI 3.1

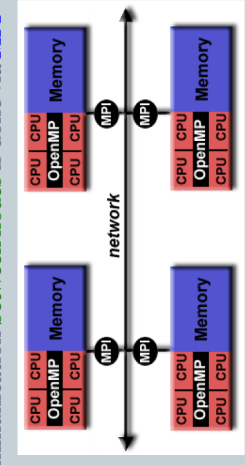


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Hybrid architectures & parallelism

Hybrid parallelism combines OpenMP threads model with the message passing (MPI) model

- threads handle *local (on-node)* data
- communication *between nodes* is done via **MPI**



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