## Computer Problems 5 and 6

## 2-D and 3-D nonlinear quasi-compressible flow

Description: Program 5 ("P5") is 2-D. Program 6 ("P6") is fully 3-D.
Due: Program 5 is due Tuesday April 16. Pgm 6 is due during finals week.
Equations for program 6 (3-D) follow. For program 5, ignore/omit all $\boldsymbol{v}$ terms and $\boldsymbol{y}$-derivatives.

## A. Equations

Program 6 has 5 unknowns: horizontal flow components ( $u$ and $v, \mathrm{~m} \mathrm{~s}^{-1}$ ), vertical flow ( $w, \mathrm{~m} \mathrm{~s}^{-1}$ ), potential temperature $(\theta$, deg. K), and perturbation pressure ( $p$ ', $P a$ ). The base-state time-invariant density ( $\bar{\rho}, \mathrm{g} \mathrm{kg}^{1}$ ) and temperature $(\bar{\theta})$ are functions of height only. The quasi-compressible set has "pseudo" sound waves traveling at speed $\mathrm{c}_{\mathrm{s}}$; the pressure approaches an anelastic solution (Droegemeier and Wilhelmson 1987, J. Atmos. Sci., p. 1187). The continuous form with advection, diffusion, pressure, \& buoyancy:

| u-momentum: | $u_{t}=-u u_{x}-v u_{y}-w u_{z}-\frac{1}{\bar{\rho}} p_{x}^{\prime}+K\left(u_{x x}+u_{y y}+u_{z z}\right)$ |
| :--- | :--- |
| $v-$-momentum: <br> (program 6 only) | $v_{t}=-u v_{x}-v v_{y}-w v_{z}-\frac{1}{\bar{\rho}} p_{y}^{\prime}+K\left(v_{x x}+v_{y y}+v_{z z}\right)$ |
| $w-m o m e n t u m: ~$ <br> $\left(\theta^{\prime}=\theta-\bar{\theta}\right)$ | $w_{t}=-u w_{x}-v w_{y}-w w_{z}-\frac{1}{\bar{\rho}} p_{z}^{\prime}+g \frac{\theta^{\prime}}{\bar{\theta}}+K\left(w_{x x}+w_{y y}+w_{z z}\right)$ |
| Perturbation <br> pressure: | $p_{t}^{\prime}=-c_{s}^{2}\left(\bar{\rho} \frac{\partial u}{\partial x}+\bar{\rho} \frac{\partial v}{\partial y}+\frac{\partial}{\partial z}(\bar{\rho} w)\right)$ |
| $\theta$ (pot.temperature): | $\theta_{t}=-(u \theta)_{x}-(v \theta)_{y}-(w \theta)_{z}+\theta\left(u_{x}+v_{y}+w_{z}\right)+K\left(\theta_{x x}+\theta_{y y}+\theta_{z z}^{\prime}\right)$ |

The discrete equations use forward time differencing for $\theta$, and centered for $\mathrm{u}, \mathrm{v}, \mathrm{w}, \mathrm{p}$ :

| u: |  |
| :---: | :---: |
| $\left\|\begin{array}{l} v: \\ (P 6) \end{array}\right\|$ |  |
| $w:$ | $\delta_{2 t} w=-{\overline{\left(\bar{u}^{z} \delta_{x} w\right)_{(n)}}}_{x}^{x}-{\overline{\left(\bar{v}^{z} \delta_{y} w\right)_{(n)}}}_{y}^{y}-\overline{\left(\bar{w}^{z} \delta_{z} w\right)_{(n)}^{z}}-\frac{1}{\overline{(\bar{\rho})}} \delta_{z} p_{(n-1)}^{\prime}+g \overline{\left(\frac{\theta^{\prime}}{\bar{\theta}}\right)_{(n)}^{z}}$ <br> (Note $\theta^{\prime} \equiv \theta-\bar{\theta}$ ) $+K_{m}\left(\delta_{x x} w+\delta_{y y} w+\delta_{z z} w\right)_{(n-1)}$ |
| $p^{\prime}$ : | $\delta_{2 t} p^{\prime}=-c_{s}^{2}\left[\bar{\rho} \delta_{x} u_{(n+1)}+\bar{\rho} \delta_{y} v_{(n+1)}+\delta_{z}\left\{\overline{\left.\left.(\bar{\rho})^{z} w_{(n+1)}\right\}\right]}\right.\right.$ (cs is the fixed sound speed) |
| $\theta$ : | P5: PL advection, plus 2-D diffusion. P6: Strang splitting + 3-D diffusion: $\left[F_{x}\left(\frac{\Delta t}{2}\right)\right]\left[F_{y}\left(\frac{\Delta t}{2}\right)\right]\left[F_{z}(\Delta t)\right]\left[F_{y}\left(\frac{\Delta t}{2}\right)\right]\left[F_{x}\left(\frac{\Delta t}{2}\right)\right]+K_{\theta}\left(\delta_{x x} \theta+\delta_{y y} \theta+\delta_{z z} \theta^{\prime}\right)_{(n)}$ |

$u, v, w$ advection follow the (unsplit) "box method," not to be confused with the implicit scheme of the same name. Pressure and diffusion terms are lagged (at time $n-1$ ). $\theta$ is advected with Lax-Wendroff or piecewise linear methods. Note: time levels, averaging!

## B. Grid layout and boundary conditions



- Dimensions:
- Use $\Delta x=\Delta z$; grid spacing, dimensions to be announced.
- We will do test cases at coarse resolution, e.g. 200 m or larger.
$\circ$ physical dimensions are no longer from (-.5,-.5) to $(+.5,+.5)$
- x coordinates (for $\left.\theta, \mathrm{p}^{\prime}\right)=\Delta \mathrm{x} / 2+\Delta \mathrm{x}(\mathrm{i}-1), \mathrm{i}=1 \ldots \mathrm{nx}$ (Fortran)
- bottom-left corner $\theta, p^{\prime}$ are at $(\mathrm{x}=\Delta x / 2, \mathrm{z}=\Delta z / 2)$
- w (at $\mathrm{k}=1$ in Fortran, $\mathrm{k}=\mathrm{K} 1$ in C ) is at $\mathrm{z}=0$
- u (at $\mathrm{i}=1$ in Fortran, $\mathrm{i}=\mathrm{I} 1$ in C ) is at $\mathrm{x}=0$
- Top, bottom boundaries:
- free slip (no drag on $u$ ); rigid lids ( $\mathrm{w}=0$ at $\mathrm{k}=1$ and $\mathrm{k}=\mathrm{nz}+1$ in Fortran)
- 0 -gradient for all variables; any variable $\xi(k=0)=\xi(\mathrm{k}=1$, Fortran $)$, etc.
- Lateral ( $x$ ) boundaries: symmetry boundaries shown with dashed yellow lines
- $\mathrm{u}(1)=-\mathrm{u}(2) \quad \mathrm{u}(\mathrm{nx}+1)=-\mathrm{u}(\mathrm{nx}) \quad$ (Fortran indices here)
- $\theta(0)=\theta(2) \quad \theta(n \mathrm{x}+1)=\theta(\mathrm{nx}-1)$ (same for $\mathrm{w}, \mathrm{p}$ ')
- Lateral (y) boundaries: (program 6, only)
- Y boundaries are periodic. Consider the periodic boundary to sit at the V wind locations for $\mathrm{j}=1$ and $\mathrm{j}=\mathrm{ny}+1$.
- You will only integrate V from 1:ny (Fortran indices); the value of V at ( $n y+1$ ) will always be set equal to V at $\mathrm{j}=1$.
- Other variables are periodic in Y as $\xi(\mathrm{ny}+1)=\xi(1)$, etc.


## C. Initial conditions (base state)

- First you must define the base state vertical profiles for density $\bar{\rho}$ and basestate potential temperature $\bar{\theta}$. You only save $\bar{\rho}$ for later use; other variables ( $\mathrm{z}, \mathrm{P}, \mathrm{T}$ ) are used only to calculate $\bar{\rho}$. There is no need to save $\mathrm{T}(\mathrm{z})$ and $\mathrm{P}(\mathrm{z})$.
- The first vertical velocity level, w at Fortran k=1, is at $\mathrm{z}=0$ consistent with our $C$-grid staggering.
- In the expressions below, $z$ refers to the height at a $\theta$ and $p$ ' level. The notation given is for Fortran.

$$
\left.\begin{array}{l}
z(k)=\frac{\Delta z}{2}+\Delta z(k-1) \\
\bar{T}(z)=300.0-\frac{g}{c_{p}} z \\
\bar{P}(z)=P_{0}(\bar{T} \overline{\bar{\theta}})^{c_{p} / R_{d}} \\
\bar{\rho}(z)=\frac{\bar{P}}{R_{d} \bar{T}}
\end{array}\right\} \text { where }\left\{\begin{array}{l}
z=\text { height }(\mathrm{m}) \text { of } \theta, u, p^{\prime} \text { levels } \\
\bar{\theta}(z)=300 K=(\text { constant }) \text { potential temperature } \\
g=9.81 \mathrm{~ms}^{-2}=\text { gravity } \\
\mathrm{c}_{\mathrm{p}}=1004 \mathrm{~J} \mathrm{~kg}^{-1} \mathrm{~K}^{-1}=\text { specific heat at constant pressure } \\
R_{d}=287 \mathrm{~J} \mathrm{~kg}^{-1} \mathrm{~K}^{-1}=\text { dry air gas constant } \\
\mathrm{P}_{0}=10^{5} \mathrm{~Pa}=\text { standard pressure at sea level } \\
\bar{\rho}=\operatorname{density}\left(\mathrm{kg} \mathrm{~m}^{-3}\right) \text { at } \theta, \mathrm{u}, \mathrm{p}^{\prime} \text { levels }
\end{array}\right.
$$

Check your initial state with this data for $\Delta \mathrm{z}=100 \mathrm{~m}$, at (Fortran) $\mathbf{k}=\mathbf{1 1}, \mathrm{z}=1050 \mathrm{~m}$ :

- $\mathrm{P}=88540 \mathrm{~Pa}$
- $\mathrm{T}=289.74 \mathrm{~K}$
- $\rho_{\text {ulevel }}=1.065 \mathrm{~g} \mathrm{~kg}^{-1}, \rho_{w_{\text {level }}}=1.069 \mathrm{~g} \mathrm{~kg}^{-1}$.
- Note you compute $\rho_{u}$ level as above, and average in height to get $\rho_{w}$ level; this

- $\rho_{w}$ level at $\mathrm{k}=1$ can have any value; it is only used where multiplied by w , and $\mathrm{w}_{\text {ground }}=0$.


## D. Initial conditions (perturbation potential temperature and $\mathbf{u}, \mathbf{w}$ )

Program 5: The solution evolves from an initial state with zero mean flow $\mathrm{U}(\mathrm{z})$ and constant potential temperature $(\theta)$. We begin with temperature perturbations: where $\theta^{\prime}$ is warm (cool) the air will rise (sink). The initial $u$, $w$, and $p$ ' are zero. For $\theta$, use:

$$
\theta_{i, k}=\bar{\theta}+\sum_{m=1}^{2}\left[\Delta \theta_{m}^{\prime} \frac{\cos \left(r_{m} \pi\right)+1}{2} \text { if } r_{m} \leq 1, \text { else } 0\right], r_{m}=\sqrt{\left(\frac{x_{i}-x_{0}(m)}{\text { xradius }}\right)^{2}+\left(\frac{z_{k}-z_{0}(m)}{\text { zradius }}\right)^{2}}
$$

so $\theta(\mathrm{i}, \mathrm{k})$ at time $\mathrm{t}=0$ equals the base state (constant) $\bar{\theta}$ plus any perturbation $\Delta \theta^{\prime}(\mathrm{m})$, for up to two initial temperature perturbations $m=1,2$.

Structure your IC code for setting up $\theta$ like that given below. The example code is for program 6, in 3-D; simplify appropriately for program 5:
distance / radius calculations for initial condition of programs 5, 6

| Fortran | C requires <math.h> |
| :---: | :---: |
|  | ```for (i=I1; i<=I2; i++) \{ for (j=J1; j<=J2; j++) \{ for ( \(k=K 1\); \(k<=K 2 ; k++\) ) \{ \(x=d x / 2.0+d x *(f l o a t)(i-I 1) ;\) \(y=d x / 2.0+d x *(f l o a t)(j-J 1) ;\) \(z=d x / 2.0+d x *(f l o a t)(k-K 1) ;\) for ( \(m=0\); \(m<2\); \(m++\) ) \{ rm \(=\) sqrt \((\) pow ( ( \(\mathrm{x}-\mathrm{x} 0[\mathrm{~m}]) / \mathrm{xradius}[\mathrm{m}], 2.0)\) +pow ( \((\mathrm{y}-\mathrm{y} 0[\mathrm{~m}]) / \mathrm{yradius}[\mathrm{m}], 2.0)\) +pow ((z-z0[m])/zradius[m],2.0)); if (rm <= 1.0) \{ /* your \(\theta\) code here */ \} /* rm */ \} /* m */``` |
| ```! ...your 0 code here... endif enddo (+3 more enddo's)``` | $\begin{aligned} & \text { \} /* k */ } \\ & \} / \star j^{*} / \\ & \} \text { /* i */ } \end{aligned}$ |

These two thermal perturbations $\Delta \theta^{\prime}$ have different center ( $\mathrm{x}, \mathrm{z}$ ) coordinates. The xand z-"radius" may vary between perturbations, so you must store two sets of "radii" .

Program 6, only: In P6, perturbations have 3-D center positions (x,y,z). You will also create perturbations to the $\mathbf{v}$ flow component, using the same code as for $\theta$ :
$\left.\begin{array}{|l}\theta_{i, j, k}=\bar{\theta}+\sum_{m=1}^{2}\left[\Delta \theta_{m}^{\prime} \frac{\cos \left(r_{m} \pi\right)+1}{2} \text { if } r_{m} \leq 1, \text { else } 0\right] \\ v_{i, j, k}=\quad \sum_{m=1}^{2}\left[\Delta v_{m} \frac{\cos \left(r_{m} \pi\right)+1}{2} \text { if } r_{m} \leq 1, \text { else } 0\right]\end{array}\right] r_{m}=\sqrt{\left(\frac{x_{i}-x_{0}(m)}{\text { xradius }_{m}}\right)^{2}+\left(\frac{y_{j}-y_{0}(m)}{\text { yradius }_{m}}\right)^{2}}$

Calculate $r_{m}$ for each point ( $\mathrm{i}, \mathrm{j}, \mathrm{k}$ ), and use it in the computation of both perturbation $\theta$ and v -wind (ignore staggered grid positions in doing so; use the same $r_{m}$ value, code).

In program 6, we also utilize random initial $\mathbf{u}$ values, up to +/-(upertur/2). Use the default Intel Fortran/C random number generator. Here is sample code:

| Fortran | C requires <math.h> |
| :---: | :---: |
| real upertur, rand | float upertur; |
| call srand (0.0) | srand (0.0); /* seed */ |
| do $k=1, n z$ | for (i=I1+1; i<=I2; i++) \{ |
| do j = 1, ny | for (j=J1; j<=J2; j++) \{ |
| do $i=1, n x+1$ | for (k=K1; k<=K2; $k++$ ) \{ |
| ul (i,j,k) = \& | u1[i][j][k] = upertur * ( |
| (rand (0)-0.5) *upertur enddo | ```(float)rand()/(RAND_MAX + 1.0) ) - upertur*0.5;``` |
| enddo | \} |
| enddo | \} \} |

## E. Code layout

The code layout guidelines include those from past programs plus the following:

- Do not put your integration (advection, diffusion, pressure gradient, buoyancy, initialization...) steps in your main program; put each in a separate subroutine. You must also use (to build your program) and submit (for grading) a makefile.
- Read in from the keyboard or a file, or use via a Fortran namelist:
- times to plot (or, a plotting interval) • temperature perturbations and their center locations ( $\mathrm{x}, \mathrm{z}$ or $\mathrm{x}, \mathrm{y}, \mathrm{z}$ ) • diffusion coefficients $\mathrm{K}_{\mathrm{m}}$ and $\mathrm{K}_{\text {theta }}$.
- Use ghost zones as before, as needed for the numerical schemes being applied.
- Set up the initial conditions (1-D for density, and 2-D or 3-D fields) entirely in one subroutine. Plot the initial potential temperature perturbation $(\theta-\bar{\theta})$.
- You must put common processes for different variables in the same subroutines: advection ( $u, \mathrm{w}, \theta$ ) (with 1-D advection still handled by a separate 1D routine); diffusion (u,w, $\theta$ ), and pressure gradient force/buoyancy ( $u, w, p$ ').
- Your main program must ONLY read input data, print out information as desired and call subroutines. All other code must be in subroutines for full credit.
- Remember $w=0$ at the top and bottom levels ( $\mathrm{k}=1$ and $\mathrm{k}=\mathrm{nz}+1$ in Fortran). So you do z mixing for $w$ only from $\mathrm{k}=2: \mathrm{nz}$ (in Fortran).
- Don't evolve $u$ outside of the symmetry boundaries; compute $\mathrm{u}(2 \ldots \mathrm{nx})$ and then determine $u(1)$ and $u(n x+1)$ using the (a)symmetric boundary conditions.
- For pressure, first compute new values for $u$ and $w$ at time level $(\mathrm{n}+1)$. Then update the pressure from $(\mathrm{n}-1)$ to $(\mathrm{n}+1)$ using $\mathrm{u}^{(\mathrm{n}+1)}$ and $\mathrm{w}^{(\mathrm{n}+1)}$ to get $\mathrm{p}^{(\mathrm{n}+1)}$.
- The order of computation is: advection ( $u, w, \theta$ ); diffusion, and pressure terms.
- Use a forward time step to start the integration (there is a short cut we'll discuss).
- Program 6 only: For full credit, you must make a reasonable attempt at parallelizing your code, and part of your grade also requires visualization.


## F. Plotting

Program 5: plot contours as usual. We will not use surface plotting.
Program 6: You will not be calling plot routines directly from your program \#6. Doing so is slow and wasteful considering how long your programs will (at full resolution) take to rerun. Instead, you will call C or Fortran routine putfield (provided to you) to write your output to disk in a unformatted binary file. Use program plot3d to read this file and to make any number of plots (X-Y, Y-Z, X-Z slices, or 3-D). See the class web page for details. These routines, program plot $3 d$ and demonstration programs will be available on stampede at $\sim \operatorname{tg} 457444 / 502 / P g m 6$. Required plots will be listed on the class web site.

## G. Hints

- Do initial testing at reduced resolution, e.g. $\Delta \mathrm{x}=\Delta \mathrm{z}=200 \mathrm{~m}, \Delta \mathrm{t}=0.5 \mathrm{~s}$.
- In testing (for Fortran), do early tests compiling with subscript checking: -g-check all-traceback.
- Beware! NX $\neq \mathbf{N Z}$ here. Think where you have used NX=NZ in programs 2-4.
- For $\min / \mathrm{max}$ stats and plotting, average $u$ and $w$ to $\theta / \mathrm{p}$ locations; and plot $(\theta-\bar{\theta})$
- We are using forward time differencing for $\theta$ advection, and centered time for everything else. So, $\delta_{2} \mathrm{u}$ means $\mathrm{u} 3=\mathrm{u} 1+2 \Delta \mathrm{t}^{*}(\ldots) ; \theta$ advection is forward in time, so only two arrays are needed [handled as in programs 2-4].


## H. Checking your code

There are various checks you could carry out to test parts of your code. Some tests you could perform include:

1. Linear advection: observe movement of $\theta^{\prime}$ field with constant $u$ and/or $w$ fields while disabling diffusion, buoyancy and pressure gradient terms.
2. 1-D: reduce two-dimensional initial condition to 1-D (e.g. let $\theta$, u , or w vary as $\sin (\mathrm{x})$ ) for advection tests.
3. Diffusion only: disable advection, buoyancy and pressure gradient terms, and damp only $\theta$ or some pre-determined function of $u$ or $w$.
4. Pressure gradient and buoyancy terms, only: disable advection and diffusion, and integrate using the pressure gradient terms (influences $u, w$ ), buoyancy term (influences $w$ ), and the pressure field update itself (from gradients in $u, w$ ). In this test, the $\theta$ field stays constant with time, and a circulation develops in the $u$ and $w$ fields. This is a particularly useful test. The sequence of evolution to look for is:
a. The temperature perturbation $\theta^{\prime}$ leads to vertical acceleration, changing $w$
b. The new, nonzero $w$ field creates pressure gradients (from $\partial \mathrm{w} / \partial \mathrm{z}$ )
c. The pressure gradients lead to horizontal acceleration, changing $u$
5. Look for symmetry in your solutions. For example, an initial temperature perturbation placed at the very center of the domain will lead to minima and maxima of opposite sign in $u$; this should remain true as your solution evolves.
a. But: the symmetry is in x ; comparable symmetry will not occur in z due to the density variation with height.

## I. Visualization (program 6 only)

Use program plot3d, provided to you, to produce the necessary contour plots. Beyond this, part of the program grade (see below) involves creating a few 3-D plots with the visualization tools vis5d or VisIt. plot3d can convert your simulation output to the necessary format. See the class web site for details.

Following is a broad description of how my program is coded.

| 1. MAIN PROGRAM <br> a. read in parameters; call IC <br> b. plot initial condition <br> c. call MAXMIN <br> d. call $\boldsymbol{B C}$ <br> e. $\quad$ set tstep $=\Delta t$ <br> f. TIME LOOP: $n=1$,max_steps <br> - $\quad$ set $\mathrm{u} 3=\mathrm{u} 1, \mathrm{w} 3=\mathrm{w} 1, \mathrm{t} 2=\mathrm{t} 1$ <br> - call ADVECT <br> - call DIFFUSION <br> - call PGF <br> - array update <br> - if $(\mathrm{n}=1)$ set tstep $=2 \Delta \mathrm{t}$ <br> - call BC <br> - call MAXMIN <br> - if desired time: PLOT <br> g. END OF TIME LOOP <br> h. plot time traces | NOTES <br> Always plot $\boldsymbol{\theta}$, not total $\boldsymbol{\theta}$ <br> Find min, max of all fields <br> Set ghost points for first time step <br> Because your first step is a forward one <br> Array copy helps start this time step. <br> Advection of $\boldsymbol{\theta}, \mathrm{u}$, and w . <br> Mix: $\mathbf{u}, \mathrm{w}$, and $\boldsymbol{\theta}$ (note: in general $K_{m} \neq K_{\text {theta }}$ ) <br> Obtain u3,w3; get new p3 <br> This is the usual array switch between old, new time levels. There are three time levels for $\mathrm{u}, \mathrm{w}, \mathrm{p}$, and two for $\boldsymbol{\theta}$. <br> But: if first step, don't update $\mathrm{u} 1, \mathrm{w} 1$, or p 1 . <br> Switch from forward to centered time for $u, w, p$. <br> Get BCs ready for next time step. $\ldots$ also store $\max / \mathrm{min}$ info for later use. Call contour routine for $\mathrm{u}, \mathrm{w}, \boldsymbol{\theta}$, and p <br> .. using $\min / \mathrm{max} u / w / \theta$ I have already stored |
| :---: | :---: |
| 2. IC ROUTINE <br> a. compute 1D arrays <br> b. $\quad$ set $p^{\prime}, u, w=0$ <br> (in program 6, we set $v$ using perturbations, and set $\boldsymbol{u}$ to random numbers; $u$ is nonzero in P6!) <br> c. set $\boldsymbol{\theta}$ based on handout. | Compute constants and 1D arrays here. includes $\operatorname{density}(\mathrm{z})$ at $\boldsymbol{\theta}$ and w levels Do this for ( n ) and ( $\mathrm{n}-1$ ) variables; this is part of preparing for the first, forward time step (hence tstep is first set to $\Delta t$, and later to $2 \Delta t$ ) Remember you read in the temperature perturbations and their locations |
| 3. BC ROUTINE <br> a. 0-gradient top, bottom <br> b. w, $\boldsymbol{\theta}$, and $\mathrm{p}^{\prime}$ are same on either side of symmetry boundary <br> c. Anti-symmetry for u | $\begin{aligned} & \text { So } u(i, n z+1)=u(i, n z) \\ & \text { So } p(0, k)=p(2, k) \text {, } \\ & \quad p(n x+1, k)=p(n x-1, k) \\ & \text { So } u(1, k)=-u(2, k), u(0, k)=-u(3, k) \end{aligned}$ |
| 4. ADVECT ROUTINE <br> a. $\boldsymbol{u}: \mathrm{u} 3=\mathrm{u} 3+$ tstep*(box terms) <br> b. $\boldsymbol{w}: \mathrm{w} 3=\mathrm{w} 3+$ tstep* (box terms) <br> c. $\theta$ advection as usual (old "integrate" code) | Recall u,w,p have centered time derivatives. For program 6, do $v$ advection here, too. <br> Piecewise linear advection. |
| 5. DIFFUSION ROUTINE <br> a. $\mathrm{u} 3=\mathrm{u} 3+$ tstep* $(\mathrm{x}, \mathrm{z}$ mixing terms) <br> b. $\mathrm{w} 3=\mathrm{w} 3+$ tstep* $(\mathrm{x}, \mathrm{z}$ mixing terms $)$ <br> c. $\operatorname{Mix} \theta \ldots$ | For program 6, do $\boldsymbol{v}$ diffusion, too. W is always zero at $\mathrm{k}=1$ and at $\mathrm{k}=\mathrm{nz}+1$ |
| 6. PGF SUBROUTINE <br> a. u3 = u3- tstep*(pgf terms) <br> b. $\mathrm{w} 3=\mathrm{w} 3-$ tstep $^{*}(\mathrm{pgf}$ terms $)$ + tstep*(buoyancy terms) <br> c. set $\mathrm{u}, \mathrm{w}$ BCs (could call $B C$, or set here) <br> d. $\mathrm{p} 3=\mathrm{p} 1-(\mathrm{pgft}$ terms $)$ | Pressure gradient / buoyancy routine. Adding to the u3 array. Adding to the w3 array. Remember $\mathrm{w}=0$ at $\mathrm{k}=1$ and $\mathrm{k}=\mathrm{nz}+1$ <br> Get ready for derivatives in p equation pgf terms use new $u$, $w$ at time ( $\mathrm{n}+1$ ) |



